

Spin-Reorientation and Weak Ferromagnetism in Antiferromagnetic

TbMn_{0.5}Fe_{0.5}O₃

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Orthorhombic single crystals of TbMn_{0.5}Fe_{0.5}O₃ are found to exhibit spin-reorientation, magnetization reversal and weak ferromagnetism. Strong anisotropy effects are evident in the temperature dependent magnetization measurements along the three crystallographic axes **a**, **b** and **c**. A broad magnetic transition is visible at $T_N^{\text{Fe/Mn}} = 286$ K due to paramagnetic to $A_x G_y C_z$ ordering. A sharp transition is observed at $T_{SR}^{\text{Fe/Mn}} = 28$ K, which is pronounced along **c** axis in the form of a sharp jump in magnetization where the spins reorient to $G_x A_y F_z$ configuration. The negative magnetization observed below $T_{SR}^{\text{Fe/Mn}}$ along **c** axis is explained in terms of domain wall pinning. A component of weak ferromagnetism is observed in field-scans along **c**-axis but below 28 K. Field-induced steps-like transitions are observed in hysteresis measurement along **b** axis below 28 K. It is noted that no sign of Tb-order is discernible down to 2 K. TbMn_{0.5}Fe_{0.5}O₃ could be highlighted as a potential candidate to evaluate its magneto-dielectric effects across the magnetic transitions.

I. INTRODUCTION

$R\text{FeO}_3$ and $R\text{MnO}_3$ (R = rare earth) perovskites exhibit multiferrocity^{1,2}, spin-switching^{3,4}, magneto-optic⁵ and magneto-electric⁶ properties which are desirable in device application. It is only natural to try and combine the most desirable features of these two classes of compounds in composite solid solution. The magnetic properties of multiferroic $R\text{MnO}_3$ (R = Tb, Dy and Gd) are well documented^{2,7}. It is now well established that switchable ferroelectric polarization in $R\text{MnO}_3$ results from the incommensurate magnetic order. On the other hand, in orthorhombic $R\text{FeO}_3$, non-collinear antiferromagnetic (AFM) G -type order of Fe^{3+} leading to weak-ferromagnetism (WFM) is observed at high temperature ($\gtrsim 300$ K) while the R sub-lattice orders antiferromagnetically at very low temperature ($\lesssim 10$ K)^{8,9}. Orthoferrites are also known to display spin-reorientation transitions. For instance DyFeO_3 shows Morin transition¹⁰ where Fe^{3+} spin system reorients from AFM configuration along **a** axis with WFM component along **c** axis to simple AFM along **b** axis at ~ 35 K¹¹. The spin-transitions are advantageous when considering the magneto-electric properties because the anisotropic magnetic properties and lattice strain can be coupled in a ferroelectric material.

In TbFeO_3 , $4f$ -electron based Tb sub-lattice and $3d$ -electron based Fe sub-lattices are coupled in anti-parallel manner. Fe^{3+} moments possess Γ_4 ($G_x A_y F_z$) order with $T_N^{\text{Fe}} \approx 650$ K¹²⁻¹⁴ accompanied by spin re-orientation to Γ_2 ($G_z C_y F_x$). At 3 K, another spin re-orientation occurs and the Fe^{3+} moments adopt Γ_4 ($G_x A_y F_z$) structure again. In the 10 - 3 K interval, the Tb^{3+} moments are

ordered in Γ_2 ($F_x C_y$) spin structure. Below 3 K, Tb^{3+} order cooperatively in Γ_8 ($A_x G_y$) configuration. TbMnO_3 , on the other hand is a well known multiferroic². It exhibits three magnetic transitions at 42 K, 28 K and 8 K. At 42 K, Mn^{3+} moments form sinusoidal incommensurate AFM order^{2,15}. The magnetic order become commensurate and generates a spiral order in **bc** plane below 28 K, this accompanies ferroelectric order along the **c** axis which is switchable to **a** axis by applying magnetic field². One would expect that a 50:50 solid solution of TbFeO_3 and TbMnO_3 might be appropriate to combine the desirable properties of both compounds into one, especially considering the example of magneto-dielectric properties generated in $\text{YFe}_{1-x}\text{Mn}_x\text{O}_3$ ⁶. Here, we present the spin-reorientation and magnetization reversal in $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ single crystals. Our studies indicate that strong anisotropic magnetic properties emerge in the half-doped crystals, disparate from both parent compounds.

II. EXPERIMENTAL

Single crystals of $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ used in this study were grown by float-zone technique employing a four-mirror image furnace (FZ-T-10000-H-VI-VP from Crystal Systems Inc., Japan). Phase purity and crystal structure of the sample was confirmed by powder X-ray diffraction patterns from crushed crystal pieces. The powder diffractograms were obtained using a Phillips X'Pert High Score instrument using $\text{CuK}\alpha$ radiation. Magnetic measurements were performed using a commercial Magnetic Property Measurement System from Quantum Design Inc. Specific heat was measured under zero applied field using a Physical Property Measurement Sys-

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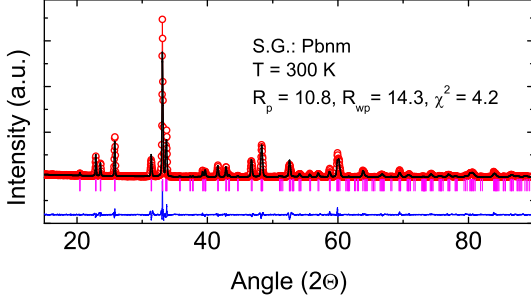


FIG. 1. (colour online) Powder x-ray diffraction pattern obtained on crushed single crystals of $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ at 300 K. Rietveld refinement results performed using $Pbnm$ space group are also presented. The goodness-of-fit was $\chi^2 = 4.2$.

III. RESULTS AND DISCUSSION

The powder diffraction data obtained on crushed single crystal samples was refined using Rietveld method¹⁶ implemented in FULLPROF code¹⁷. The refined structural parameters using $Pbnm$ space group are collected in Table I and the refined pattern showing the observed, calculated data and the Bragg reflections is shown in Fig. 1. The refinement was carried out in the space group $Pbnm$. The quality measures obtained are: $R_p = 10.8$, $R_{wp} = 14.3$, and $\chi^2 = 4.2$. A single crystal was oriented in three different crystallographic directions **a**, **b** and **c** with the help of Laue camera for magnetic measurements.

Temperature dependent magnetization measurements were carried out on oriented single crystals along **a**, **b** and **c** axes in a Quantum Design Inc. SQUID magnetometer. Fig 2(a) and (b) present the data in zero field cooled (ZFC) and field-cooled cooling (FCC) protocols at 100 Oe, respectively. In $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$, the first magnetic transition while cooling from 300 K is observed near 286 K; denoted as $T_N^{\text{Fe/Mn}}$ (highlighted in the inset of Fig 2 (a)). Upon Mn-doping, the general trend observed in rare earth orthoferrites is a reduction of T_N and an enhancement of $T_{SR}^{\text{Fe/Mn}}$ ^{18–20}. When the Mn doping level

TABLE I. The structural details of $\text{TbFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ obtained by refining powder x-ray diffraction data at 300 K using $Pbnm$ space group. The refined lattice parameters are $a = 5.311(7)\text{\AA}$, $b = 5.697(2)\text{\AA}$ and $c = 7.539(3)\text{\AA}$.

Atom	Wyckoff pos.	x/a	y/b	z/c
Tb	4c	-0.0155(2)	0.0729(3)	0.25
Mn/Fe	4b	0.5	0	0
O1	4c	0.1138(3)	0.4629(2)	0.25
O2	8d	0.6997(4)	0.3096(2)	0.0586(1)

is near 50%, T_N and $T_{SR}^{\text{Fe/Mn}}$ would be very close to each other¹⁸. For example, in $\text{DyFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$, the transition temperatures are $T_N^{\text{Fe/Mn}} = 320$ K and $T_{SR}^{\text{Fe/Mn}} = 310$ K respectively for $x = 0.5$ ¹⁹. The transition at 286 K in $\text{TbFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ is identified as a paramagnetic-to-AFM transition. The transition is more clearly shown in the inset of (b) where a plot of dM/dT versus T is plotted.

A second magnetic phase transition is observed for $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ at 28 K as a sharp feature along all the crystallographic directions (Fig 2 (a) and (b)). However, this transition is most pronounced for the **c**-axis. At this temperature denoted by $T_{SR}^{\text{Fe/Mn}}$ to signify a spin-reorientation transition, the magnetic structure of $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ changes from $A_xG_yC_z$ (or simply G_y because A_x and C_z components are very small) to $G_xA_yF_z$. G_y is chosen from the magnetic symmetry consideration²¹ and the fact that there is no hysteresis loop at 250 K, below $T_N^{\text{Fe/Mn}}$ in any direction. In most $R\text{FeO}_3$ compounds, Fe^{3+} orders in $G_xA_yF_z$ configuration below T_N ⁹. In TbMnO_3 , Mn^{3+} moments adopt an incommensurate spiral order at low temperature however, Tb also orders at very low temperatures below ≈ 7 K. It is natural to assume that the spin-reorientation transition in $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ would depend on the competi-

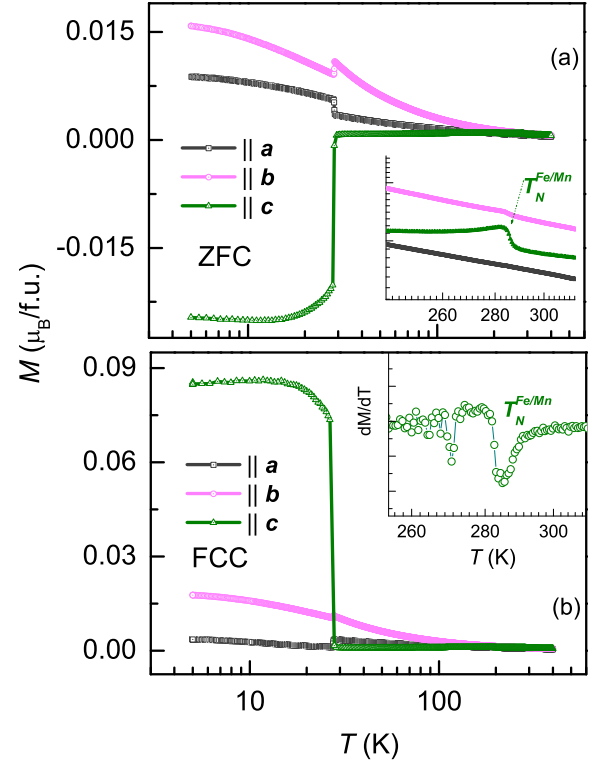


FIG. 2. (colour online) (a) ZFC curves at 100 Oe along three crystallographic axes, **a**, **b** and **c**. The inset shows a magnified view of the high temperature region where the transition at $T_N^{\text{Fe/Mn}} = 286$ K along **c** axis is evident. (b) FCC curves along different axes. The inset magnifies the high temperature region around $T_N^{\text{Fe/Mn}}$.

tion between the magnetic anisotropy energies of Mn^{3+} and Fe^{3+} . At 28 K the anisotropy energy of Fe^{3+} will be overcome by that of Mn^{3+} ions and consequently, a $G_x A_y F_z$ configuration with a WFM component along \mathbf{c} -axis results. It must be noted that in TbMnO_3 , the Mn^{3+} ions order AFM along \mathbf{b} -axis below 28 K. Further support for the arguments about the nature of phase transitions at $T_N^{\text{Fe/Mn}}$ and $T_{SR}^{\text{Fe/Mn}}$ would follow from the hysteresis measurements presented in subsequent sections.

In Fig 2 (a), negative magnetization is observed for the magnetization data measured along \mathbf{c} -axis. The observed negative magnetization can be explained in terms of the domain wall pinning model described in the next paragraph. Spin reversal and negative magnetization are observed in SmFeO_3 ²² or NdFeO_3 ⁴ where, a spontaneous spin reversal of the Fe/Mn and R sub-lattices leads to the first-order jump in magnetization. The phenomena of negative magnetization is well documented in recent reviews²³ and note that care must be exercised in explaining its origins. Rare earth ordering in $R\text{FeO}_3$ or $R\text{MnO}_3$ is reflected as an anomaly in magnetization below 4 K along \mathbf{a} and \mathbf{b} axis⁷⁻⁹. In $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ a weak, broad cusp is seen at 12 K in the magnetization measured along \mathbf{c} axis. However, this cannot be accounted in terms of Tb ordering as Tb usually orders below 8.5 K with the spins confined in the \mathbf{ab} plane¹⁵. Curie-Weiss analysis of the magnetization data along three axes reveals FM interaction along \mathbf{b} -axis and AFM components along the other two axes as listed in Table II.

FCC and field-cooled warming (FCW) magnetization measurements performed at 100 Oe along \mathbf{c} -axis (denoted as M_c) after oscillating the field from 30 kOe and making the field minimum and positive are presented in Fig 3 (a) along with the corresponding ZFC curve. M_c exhibits contrasting temperature dependence in ZFC and FCC data. Clear irreversibility is seen between the FCC and FCW curves close to $T_{SR}^{\text{Fe/Mn}}$ (inset of fig 3 (a)), where M_c changes from -0.02 to $+0.0017 \mu_B/\text{f.u.}$ The transition width (ΔT) is about 2 K. The negative magnetization for M_c could be explained in terms of domain wall pinning. Since Tb moment have no FM component along \mathbf{c} -axis for either of the parent compounds, a competition between $4f$ moment and $3d$ moments could be excluded. During ZFC measurements, magnetic moments are likely to align according to the anisotropy and internal magnetic exchanges and magnetic domains can form along different directions. Depending upon the initial configuration of the domains and strength of domain wall pinning even an overall negative magnetization could result. When the temperature increases in the ZFC measurements more and more domains align towards the field but still with an overall negative magnetization. This explains the gradual increase in M_c till $T_{SR}^{\text{Fe/Mn}}$. At 28 K the spin structure reorient to G_y . In FCW measurements, most of the domains are aligned towards the applied field giving a positive total magnetic moment. With increase in temperature, M_c shows moderate decrease up to $T_{SR}^{\text{Fe/Mn}}$

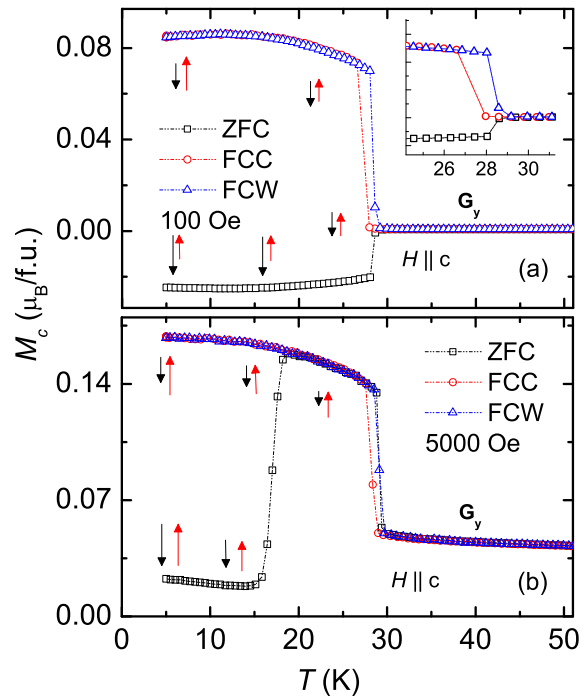


FIG. 3. (colour online) (a) ZFC, FCC and FCW measurements at 100 Oe along \mathbf{c} axis. (b) represents same set of measurements performed at 5000 Oe. The data shown is limited upto 50 K. Inset shows the thermal hysteresis seen at $T_{SR}^{\text{Fe/Mn}}$ transition. Data collected upon warming are shown in blue, and upon cooling in red. A schematic representation of the magnetic domain strength along and opposite to the applied field are drawn as red and black arrows, respectively.

TABLE II. Effective paramagnetic moments and Curie-Weiss temperatures of $\text{TbMn}_{0.5}\text{Fe}_{0.5}\text{O}_3$ extracted from performing Curie-Weiss analysis of the magnetization data along the three different axes.

	a	b	c
$\mu_{\text{eff}} (\mu_B/\text{f.u.})$	9.35(3)	10.75(1)	13.11(3)
$\Theta_{CW} (\text{K})$	-5.5(2)	15.3(4)	-227.5(2)

due to the decrease in domain strength of those domains oriented opposite to the field. At $T_{SR}^{\text{Fe/Mn}}$, M_c shows a sudden fall from 0.07 to $0.0017 \mu_B/\text{f.u.}$ The sudden fall could be because of the spin-reorientation back to the G_y configuration. Apart from the usual spin-reorientation, a total magnetization reversal is observed in NdFeO_3 and SmFeO_3 ⁴ similar to the present case. The competition between rare earth $4f$ sub-lattice and transition element $3d$ sub-lattice in $R\text{FeO}_3$ plays a major role in the spin-reorientation transition⁴.

M_c was measured at higher applied magnetic field to check if the spin-reorientation transition changes with the magnetic field and the results are presented in Fig 3 (b). At higher applied field, negative M_c is not observed, but the overall nature of M_c is similar to that

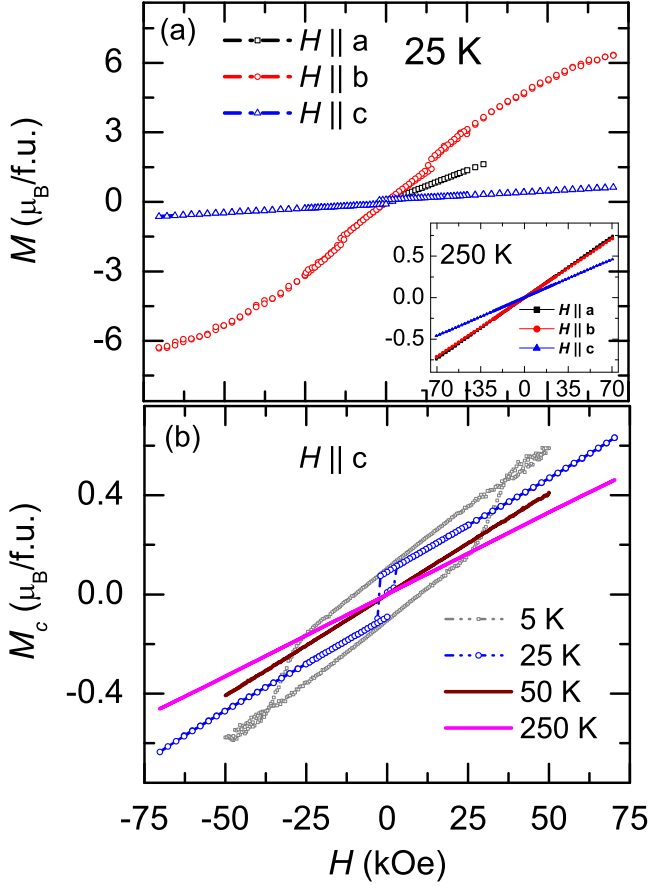


FIG. 4. (colour online) (a) Field-scans of magnetization, $M(H)$, along a , b and c axis at 25 K and 250 K (inset). Anomalies (step-like) are observed in the b -axis data at ≈ 25 kOe. (b) $M(H)$ along c axis at different temperatures. A weak component of ferromagnetism is revealed at low temperatures.

measured at 100 Oe. In case of ZFC, even though domains with a resultant orientation opposite to the applied field are present, an overall positive moment is observed. This is due to the fact that at a higher applied field, more domains will orient towards the field. With increase in temperature more and more domains align towards the field and at a critical temperature (~ 16 K) most of the domains are orient towards the field. In the FCC and FCW measurements most of the domains are already oriented along the field direction and with increase in temperature the strength of the domains decreases. This explains the gradual decrease of moment till $T_{SR}^{\text{Fe/Mn}}$. The spins reorient from $G_x A_y F_z$ configuration to G_y configuration near 28 K, which explains the sudden fall in M_c . Interestingly, in the parent TbMnO_3 , AFM incommensurate-commensurate transition responsible for the ferroelectric phase is reported to happen exactly at 28 K². The sinusoidal AFM ordering is along b axis in TbMnO_3 . In $\text{RFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$, the anisotropy energy of Fe moments is overcome by that of Mn moments at a specific temperature^{18,19}. Due to high mag-

netic anisotropy of Mn moments, the Fe moments will align towards the direction of Mn moments. This normally changes the AFM direction from a axis to b axis at $T_{SR}^{\text{Fe/Mn}}$.

Field-scans of magnetization along the $H \parallel a$, $H \parallel b$ and $H \parallel c$ are shown in fig 4 (a) at 25 K while the inset shows that at 250 K. No hysteresis is observed along $H \parallel a$, $H \parallel b$ or $H \parallel c$ at 250 K. This fact confirms that the transition at 286 K is an AFM ($A_x G_y C_z$ or simply G_y) transition. At 25 K, just below the $T_{SR}^{\text{Fe/Mn}}$ transition, a hysteresis loop opens only for M_c (this is clear from the panel (b)). This indicates that at $T_{SR}^{\text{Fe/Mn}}$ magnetic structure changes from G_y to $G_x A_y F_z$ ordering with WFM along c -axis. It is understood that weak ferromagnetism is not present along a or b direction as suggested for other orthoferrites. Magnetic moment of $\sim 7.5 \mu_B/\text{f.u.}$ is observed at high field for magnetization measured along b -axis. The high value of moment along a and b -axes is from a possible $F_x C_y$ -like ordering of Tb^{3+} moments as seen in the parent compound, TbFeO_3 ¹⁴. A first-order spin-flip transition occurs at $H_c \pm 26$ kOe evident in the b -axis data. In the magnetization along a , no hysteresis is detected even at 2 K (not shown). Note that Table-II revealed predominant AFM interactions present along a axis. Detailed isothermal measurements are performed along c and are exhibited in fig 4 (b). Although the magnetization along a or b show no hysteresis, the magnitude of $M_a \approx 5M_c$ while $M_b \approx 10M_c$. In $H \parallel c$ measurements, a clear hysteresis loop is observed at 5 K. Even at 50 kOe, M_c is not saturated which indicates the underlying antiferromagnetic state of the compound²⁴.

Finally, the specific heat of $\text{TbFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ single crys-

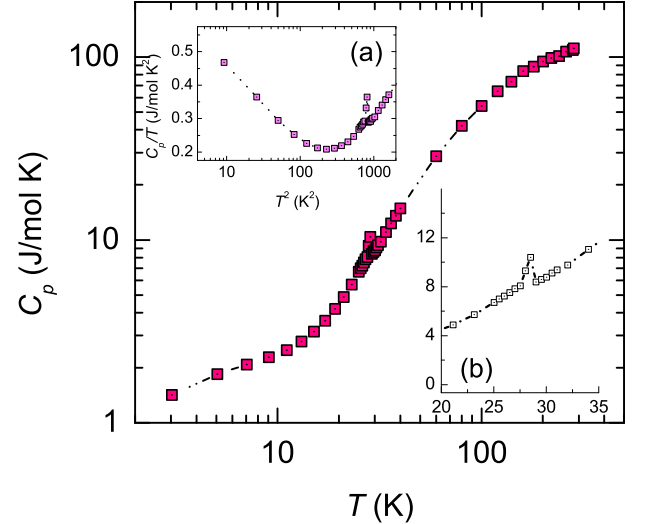


FIG. 5. (colour online) Specific heat of $\text{TbFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ single crystal at zero applied magnetic field. The inset (a) is a plot of C_p/T versus T^2 . The inset (b) shows a magnified view near $T_{SR}^{\text{Fe/Mn}}$.

tal measured using heat-pulse method in the PPMS is

presented in the main panel of Fig 5 in log-log scale. Spin-reorientation transition at $T_{SR}^{\text{Fe/Mn}}$ is clearly evident in the plot as a sharp cusp. The broad magnetic G_x transitions at $T_N^{\text{Fe/Mn}}$ is not visible as sharp transition but rather as a broad feature in the derivative, dC_p/dT (not shown). In ErFeO_3 , a distinct enhancement in specific heat value in the spin reorientation regime is reported²⁵. Inset of Fig 5 (a) shows the plot of C_p/T over T^2 . Below the transition at $T_{SR}^{\text{Fe/Mn}}$ which shows as a peak, a gradual decrease in C_p/T is observed and then eventually a sharp increase. The sharp increase at low temperature is due to the rare-earth ordering. In TbFeO_3 , Tb is reported to order at 3.2 K²⁶. The linear region below the transition was used to fit the expression $C_p = \beta_3 T^3 + \beta_5 T^5$. From this fit, the value for β is obtained to be used in the relation $\Theta_D = (\frac{12p\pi^4 R}{5\beta_3})^{1/3}$; where p is the number of atoms in the unit cell and R is the universal gas constant. Θ_D is estimated to be ≈ 480 K, matching with the value reported for TbFeO_3 by Parida et al.²⁷. A magnified view of the temperature region near T_{SF}^{Fe} is presented in the inset (b).

IV. CONCLUSIONS

The magnetic properties of single crystal $\text{TbFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ along different crystallographic axes are investigated in detail. Prominent anisotropy effects are observed. At $T_N^{\text{Fe/Mn}} = 286$ K antiferromagnetic $A_x G_y F_z$ (or simply G_y) ordering is observed which reorient to $G_x A_y F_z$ configuration below $T_{SR}^{\text{Fe/Mn}} = 28$ K. The magnetic properties of the mixed-solution $\text{TbFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$ are found to be entirely different from both the end compounds, TbMnO_3 and TbFeO_3 . Strong competition between the magnetic anisotropy energy of Fe and Mn moments make this compound magnetically complicated. A component of weak ferromagnetism is clearly revealed along c axis which also presents negative magnetization in low fields. Detailed neutron diffraction measurements and subsequent inelastic scattering experiments using single crystals are planned in order to shed more light in to the complex $H-T$ phase diagram of $\text{TbFe}_{0.5}\text{Mn}_{0.5}\text{O}_3$.

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